

## Základní Maclaurinovy rozvoje

$$\begin{aligned} \frac{1}{1-x} &= \sum_{n=0}^{+\infty} x^n &= 1 + x + x^2 + x^3 + \dots, & x \in (-1, 1), \\ (1+x)^p &= \sum_{n=0}^{+\infty} \binom{p}{n} x^n &= 1 + px + \frac{p(p-1)}{2!} x^2 + \dots, & x \in (-1, 1), \quad p \in \mathbb{R}, \\ e^x &= \sum_{n=0}^{+\infty} \frac{x^n}{n!} &= 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots, & x \in \mathbb{R}, \\ \ln(1+x) &= \sum_{n=0}^{+\infty} (-1)^n \frac{x^{n+1}}{n+1} &= x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots, & x \in (-1, 1), \\ \sin x &= \sum_{n=0}^{+\infty} (-1)^n \frac{x^{2n+1}}{(2n+1)!} &= x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots, & x \in \mathbb{R}, \\ \cos x &= \sum_{n=0}^{+\infty} (-1)^n \frac{x^{2n}}{(2n)!} &= 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \dots, & x \in \mathbb{R}, \\ \arcsin x &= \sum_{n=0}^{+\infty} \frac{[(2n-1)!!]^2 x^{2n+1}}{(2n+1)!} &= x + \frac{x^3}{6} + \frac{3x^5}{40} + \frac{5x^7}{112} + \dots, & x \in \langle -1, 1 \rangle, \\ \operatorname{arctg} x &= \sum_{n=0}^{+\infty} (-1)^n \frac{x^{2n+1}}{2n+1} &= x - \frac{x^3}{3} + \frac{x^5}{5} - \frac{x^7}{7} + \dots, & x \in \langle -1, 1 \rangle, \\ \sinh x &= \sum_{n=0}^{+\infty} \frac{x^{2n+1}}{(2n+1)!} &= x + \frac{x^3}{3!} + \frac{x^5}{5!} + \frac{x^7}{7!} + \dots, & x \in \mathbb{R}, \\ \cosh x &= \sum_{n=0}^{+\infty} \frac{x^{2n}}{(2n)!} &= 1 + \frac{x^2}{2!} + \frac{x^4}{4!} + \frac{x^6}{6!} + \dots, & x \in \mathbb{R}, \\ \operatorname{argsinh} x &= \sum_{n=0}^{+\infty} (-1)^n \frac{[(2n-1)!!]^2 x^{2n+1}}{(2n+1)!} &= x - \frac{x^3}{6} + \frac{3x^5}{40} - \frac{5x^7}{112} + \dots, & x \in \langle -1, 1 \rangle, \\ \operatorname{argtgh} x &= \sum_{n=0}^{+\infty} \frac{x^{2n+1}}{2n+1} &= x + \frac{x^3}{3} + \frac{x^5}{5} + \frac{x^7}{7} + \dots, & x \in (-1, 1). \end{aligned}$$