

OPAKOVÁNÍ

A) ROVNICE A NEROVNICE

Příklad 1. Řešte v $\mathbb{R}$:

- 1) $2x^2 - 3x - 5 = 0$ $[x \in \{-1, \frac{5}{2}\}]$
- 2) $x^2 + 2x - 15 = 0$...řešte pomocí Viètových vzorců $[x \in \{3, -5\}]$
- 3) $x^2 - |x - 1| = 1$ $[x \in \{-2, 1\}]$
- 4) $|x + 2| \geq 3$ $[x \in (-\infty, -5) \cup \langle 1, \infty)]$
- 5) $x^2 < 4$ $[x \in (-2, 2)]$
- 6) $x^2 - 5x - 6 > 0$ $[x \in (-\infty, -1) \cup (6, \infty)]$
- 7) $4^{x+1} + 8 \cdot 4^x = 12$ $[x = 0]$
- 8) $25^{-x} + 5^{1-x} = 50$ $[x = -1]$
- 9) $\log_3(x + 1) + \log_3(x + 3) = 1$ $[x = 0]$
- 10) $2^{\ln x} - 4^{\ln x} = 0$ $[x = 1]$
- 11) $3 \cotg \frac{x}{2} = -\sqrt{3}$ $[x = \frac{4}{3}\pi + 2k\pi]$
- 12) $\sin\left(x + \frac{\pi}{6}\right) = \frac{1}{2}$ $[x_1 = 2k\pi, x_2 = \frac{2}{3}\pi + 2k\pi]$

B) ÚPRAVY VÝRAZŮ

Příklad 2. Upravte výrazy na co nejjednodušší tvar:

- 1) $\frac{2x}{x+2} - \frac{6x}{6-3x} + \frac{8x}{x^2-4}$ $\left[\frac{4x}{x-2}\right]$
- 2) $\frac{\frac{x}{x-1} - \frac{x+1}{x}}{\frac{x}{x-1} - 1}$ $\left[\frac{1}{x}\right]$
- 3) $\frac{a^3 - b^3}{b^2 \left(a + \frac{1}{a+b}\right)}$ $[a^2 - b^2]$
- 4) $\left(\frac{x-1}{x-2} - \frac{x}{x-1}\right) \cdot \left(x - \frac{x}{x+1}\right) \cdot (x^2 - 1)$ $\left[\frac{x^2}{x-2}\right]$
- 5) $\frac{\frac{b}{a^2+ab} + \frac{2}{a+b} + \frac{a}{b^2+ab}}{\frac{a}{b} - \frac{b}{a}}$ $\left[\frac{1}{a-b}\right]$

$$\begin{aligned}
6) \quad & \frac{\frac{1}{x+y} + \frac{x-y}{(x+y)^2}}{1 + \left(\frac{x-y}{x+y}\right)^2} && \left[\frac{x}{x^2 + y^2} \right] \\
7) \quad & \frac{\frac{a^2+4}{a} - 2}{\left(\frac{1}{a^2} + \frac{1}{4}\right) \cdot \frac{a^3+8}{a^2+4}} && \left[\frac{4a}{a+2} \right] \\
8) \quad & \frac{\left(ab - \frac{1}{ab}\right)^2}{\left(a + \frac{1}{b}\right)^2 \cdot \left(b - \frac{1}{a}\right)^3} && \left[\frac{a}{ab-1} \right] \\
9) \quad & \frac{(x^2-y^2)^2}{x^3-y^3} \cdot \frac{x^2+xy+y^2}{x^3+y^3} \cdot \frac{1}{x^2+2xy+y^2} + \frac{\frac{1-x}{x-x^2}}{x-y+\frac{y^2}{x}} && \left[\frac{2x}{x^3+y^3} \right] \\
10) \quad & \frac{\frac{a^2+b^2}{b} + 2a}{\frac{1}{b} + \frac{1}{a}} + \frac{2b - \frac{a^2+b^2}{a}}{\frac{1}{b} - \frac{1}{a}} && [a^2 + b^2]
\end{aligned}$$

Příklad 3. Upravte výrazy na co nejjednodušší tvar:

$$\begin{aligned}
1) \quad & \frac{\cos^2 x}{1 + \sin x} && [1 - \sin x] \\
2) \quad & \frac{\sin 2x}{1 - \cos 2x} && [\cotg x] \\
3) \quad & \frac{1}{1 + \operatorname{tg}^2 x} + \frac{1}{1 + \cotg^2 x} && [1] \\
4) \quad & \frac{\sin x}{1 + \cos x} + \frac{\sin x}{1 - \cos x} && \left[\frac{2}{\sin x} \right] \\
5) \quad & \frac{1 + \cos 2x}{1 - \cos 2x} && [\cotg^2 x] \\
6) \quad & \frac{\operatorname{tg} x}{1 + \operatorname{tg}^2 x} && \left[\frac{1}{2} \sin 2x \right] \\
7) \quad & \frac{1 - \cos 2x + \sin 2x}{1 + \cos 2x + \sin 2x} && [\operatorname{tg} x] \\
8) \quad & \frac{\sin x - \sin^3 x}{\cos x - \cos^3 x} && [\cotg x] \\
9) \quad & \frac{2 \sin x - \sin 2x}{2 \sin x + \sin 2x} && \left[\operatorname{tg}^2 \frac{x}{2} \right] \\
10) \quad & \frac{\operatorname{tg} x \cdot \operatorname{tg} 2x}{\operatorname{tg} x - \operatorname{tg} 2x} && [-\sin 2x]
\end{aligned}$$